

### STOR 320 Modeling IV

Lecture 17

Yao Li

Department of Statistics and Operations Research UNC Chapel Hill



#### Introduction

- Instructions
  - Download Tutorial 13 Zip
  - Unzip Folder
  - Required Packages
    - library(modelr)
    - library(tidyverse)
    - library(purrr)
    - library(broom)
  - Open .Rmd File and Knit



#### Discussion

- Problems With Current Approach
  - Same Model For All Locations
  - Not All Locations Used in Train
  - Not All Locations Used in Test
  - Residuals Indicate that Model Can Be Improved
  - Not Helpful for Forecasting
  - Ambiguous Results: No Clear Winner

- Previously
  - Split Data in Train and Test
    - Train (28 Rivers)
    - Test (3 Rivers)
  - Purpose
    - Estimate Out-of-Sample Error
    - Pick Best Model Based on This Estimate
    - Combat Overfitting
    - Robustification
  - Goal: Find the Simplest Model that Adequately
     Predicts

- Current Issues
  - Decision on Final Model Heavily Influenced by the Test Data
  - Loss of Data in Model Fitting
  - Not Appropriate in Small Datasets
- Cross Validation Idea
  - Split Data Into Many Groups
  - Each Group Acts as a Test Set
  - All Data is Used in Both Model Fitting and Model Testing
  - Help: Chapter 5 (ISLR)

- Tidyverse Concepts
  - Chapter 20 (R4DS)
  - List-Columns
    - Columns in Data Frames or Tibbles Can Be Lists
    - What this Means
      - Column of Tables
      - Column of Models
      - Column of Functions
  - Functions
    - nest(): Converts Rows of a Data Frame into a List
    - unnest(): What do You Think It Does?

- Run Chunk 1
  - Observe the Output
  - Column of Tibbles
- Run Chunk 2
  - Imagine We Wanted to Split
    - Test: Data For Location 103
    - Train: All Remaining Data
  - Use of filter() and unnest()
  - First Glimpse -> 365 x 8
  - Second Glimpse -> 10,972 x 8

- Chunk 3
  - Run Each Line
  - What is Happening?
  - Use View() on DATA2 and Scan Through the Data
  - What do You Notice?
- Chunk 4
  - Create a Loop that Repeats this Process for Each Location
  - Each Location Is a Test Set
  - Predictions Saved are All Out-of-Sample
  - Run Chunk 4 to Test Your Code

• Chunk 4 (Continued)

```
DATA2=DATA
DATA2$linpred=NA
for(k in unique(DATA2$L)){
TEST = NEST.DATA %>% filter(L==k) %>%
unnest()
TRAIN = NEST.DATA %>% filter(L!=k) %>%
unnest()
```

```
linmod=lm(W~A, data=TRAIN)
linmodpred=predict(linmod,newdata=TEST)
```

DATA2\$linpred[which(DATA2\$L==k)]=linmodpred

- Chunk 5
  - In Our Data, We Have:
    - Actual Water Temperatures
    - Out-of-Sample Predicted Water Temperatures
  - Create RMSE.func() With Two Arguments
    - actual= vector of actual water temperatures
    - predict=vector of predicted water temperatures
  - Use This Function on the Two Columns in DATA2 for RMSE
    - actual=W
    - predict=linpred

• Chunk 5 (Continued)

```
RMSE.func = function(actual,predict){
   mse=mean((actual-predict)^2,na.rm=T)
   rmse=sqrt(mse)
   return(rmse)
}
RMSE.func(actual=DATA2$W,
        predict=DATA2$linpred)
```



RMSE.func(actual=DATA2\$W,predict=DATA2\$linpred)
] 3.147084



#### Intermission

- Current
  - Using the Natural Grouping of Data for 31-Fold Cross Validation
  - Only Fit One Linear Model
  - Should Use Cross-Validation for Multiple Different Models and Compare Cross-Validated RMSE
- Next
  - Randomly Assign Observations to *K*-Folds
  - CV Function: crossv\_kfold(*K*)

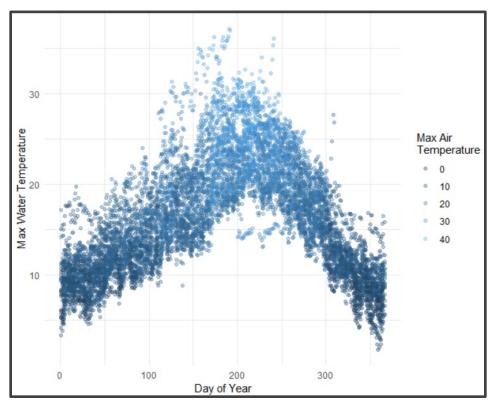


- Overview (*K*=10)
  - Randomly Split Observations Into K Groups
  - Each Fold Acts as a Test Set
  - If Each Fold Contains Approximately the Same # of Observations,





- Run Chunk 1
  - Variables (Julian Day)
  - Clear Non-Linear Relationship





#### Part 2: K-Fold CV

General Polynomial Model

$$W = a + \sum_{i=1}^{I} b_i A^i + \sum_{j=1}^{J} c_j D^j + \varepsilon$$

- Perform K-Fold CV to Estimate Out-of-Sample RMSE for Choices of *I=4* and *J=3*
- Ultimate Goal is To Select Best *I* and *J*



#### Part 2: K-Fold CV

- Run Chunk 2
  - Fit Model with *I*=4 and *J*=3
  - Functions from broom Package
    - tidy()
    - glance()

#### Used to Preview Models

tidy(polymodel) A tibble: 8 x 5						
term	estimate	std.error	statistic	p.value		
<chr></chr>	<db1></db1>	<db1></db1>	<db1></db1>	<db 7=""></db>		
(Intercept)	16.2	0.027 <u>3</u>	595.	0.		
poly(A, 4)1	328.	4.36	75.3	0.		
poly(A, 4)2	49.0	2.80	17.5	1.62e-67		
poly(A, 4)3	2.85	2.78	1.02	3.06e- 1		
poly(A, 4)4	-3.62	2.72	-1.33	1.84e- 1		
poly(JULIAN_DAY, 3)1	46.0	2.78	16.6	8.85e-61		
poly(JULIAN_DAY, 3)2	-226.	4.31	-52.5	0.		
poly(JULIAN_DAY, 3)3	-59.3	2.89	-20.5	8.66e-92		
<pre>glance(polymodel) A tibble: 1 x 11</pre>						
r.squared adj.r.squared sig	gma statisti	c p.value 🛛	df logLik	AIC BIC		
<db1> <db1> <db1> <d< td=""><td>b7&gt; <db7< td=""><td>&gt; <db1> <in< td=""><td>t&gt; <db1> &lt;</db1></td><td><db1> <db1></db1></db1></td></in<></db1></td></db7<></td></d<></db1></db1></db1>	b7> <db7< td=""><td>&gt; <db1> <in< td=""><td>t&gt; <db1> &lt;</db1></td><td><db1> <db1></db1></db1></td></in<></db1></td></db7<>	> <db1> <in< td=""><td>t&gt; <db1> &lt;</db1></td><td><db1> <db1></db1></db1></td></in<></db1>	t> <db1> &lt;</db1>	<db1> <db1></db1></db1>		
0.797 0.797 2	.71 <u>5</u> 525	. 0	8 - <u>23</u> 804. <u>47</u>	<u>626. 47</u> 691.		



- Run Chunk 3
  - Divide Data into 10 Folds
    - Use crossv\_kfold() Function
    - Variables are Lists of Train and Test Sets
  - For Each Row, We Want to Fit on Train and Predict on Test

head(DATA3) A tibble: 6 x 3						
trair	า	test		.id		
<1is	t>	<1is	t>	<chr></chr>		
<s3:< th=""><td>resample&gt;</td><td><s3:< td=""><td>resample&gt;</td><td>01</td></s3:<></td></s3:<>	resample>	<s3:< td=""><td>resample&gt;</td><td>01</td></s3:<>	resample>	01		
<s3:< th=""><th>resample&gt;</th><th><s3:< th=""><th>resample&gt;</th><th>02</th></s3:<></th></s3:<>	resample>	<s3:< th=""><th>resample&gt;</th><th>02</th></s3:<>	resample>	02		
<s3:< th=""><th>resample&gt;</th><th><s3:< th=""><th>resample&gt;</th><th>03</th></s3:<></th></s3:<>	resample>	<s3:< th=""><th>resample&gt;</th><th>03</th></s3:<>	resample>	03		
<s3:< th=""><th>resample&gt;</th><th><s3:< th=""><th>resample&gt;</th><th>04</th></s3:<></th></s3:<>	resample>	<s3:< th=""><th>resample&gt;</th><th>04</th></s3:<>	resample>	04		
<s3:< th=""><td>resample&gt;</td><td><s3:< td=""><td>resample&gt;</td><td>05</td></s3:<></td></s3:<>	resample>	<s3:< td=""><td>resample&gt;</td><td>05</td></s3:<>	resample>	05		
<s3:< th=""><td>resample&gt;</td><td><s3:< td=""><td>resample&gt;</td><td>06</td></s3:<></td></s3:<>	resample>	<s3:< td=""><td>resample&gt;</td><td>06</td></s3:<>	resample>	06		



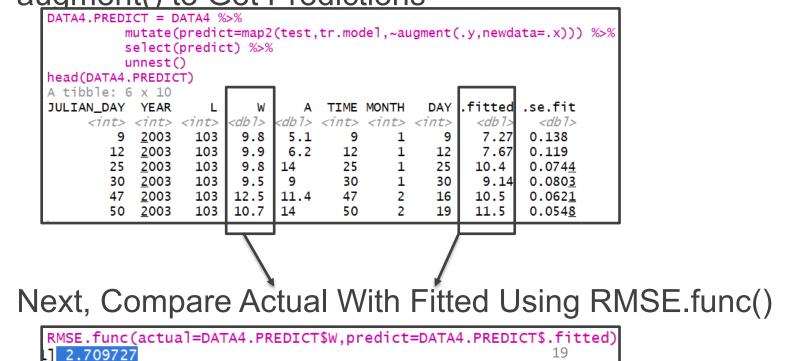
- Run Chunk 4
  - Create Function to Fit Models
  - Apply Function to All Train Sets Using purrr::map() Function

```
DATA4=DATA3 %>%
       mutate(tr.model=map(train,train.model.func,i=i,j=j))
head(DATA4)
A tibble: 6 \times 4
                            .id
                                    tr.model
train
            test
           <1ist>
                              <chr> <list>
\langle list \rangle
<S3: resample> <S3: resample> 01
                                    <S3: 1m>
<S3: resample> <S3: resample> 02 <S3: lm>
<S3: resample> <S3: resample> 03 <S3: lm>
<S3: resample> <S3: resample> 04
                                    <S3: 1m>
<S3: resample> <S3: resample> 05
                                    <S3: 1m>
<S3: resample> <S3: resample> 06
                                    <S3: 1m>
```

- Functions from purrr Package
  - map() Loop Over Train
  - map2() Loop Over Fitted Models and Test



- Run Chunk 5
  - purrr::map2() Iterates Function Over Two Arguments
  - For Every Test Set and Trained Model, We Use augment() to Get Predictions





#### Look Ahead

- What We Have Done
  - Specify I and J
  - Use 10-Fold Cross Validation to Estimate Out-of-Sample RMSE
- How We Should Use This
  - Choose Max *I* and Max *J* (Example: 10)
  - Initiate 10 x 10 Matrix of NA
  - Loop Through All *i* and *j* to Capture Out-of-Sample RMSE
  - Create a Tile Plot that Visualizes the RMSE for Each Combination of *i* and *j*
  - Choose Best *i* and *j*